

Quantum transport in ultra-short channel VLSI CMOS-Transistors

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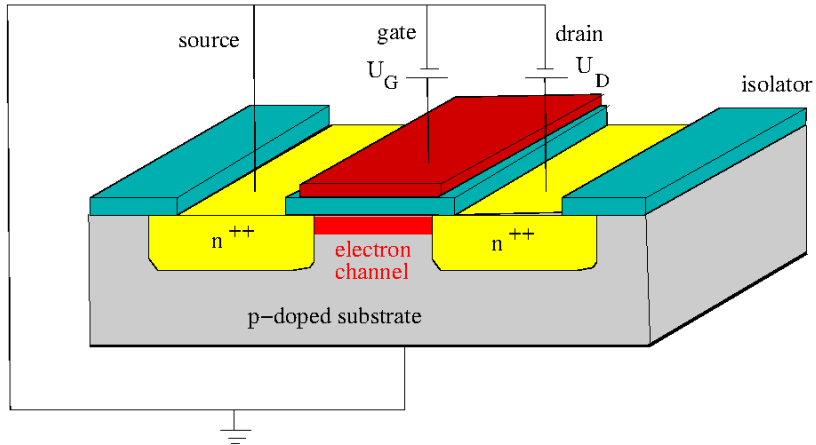
J. Höntschel and M. Horstmann
GLOBALFOUNDRIES Dresden

A contribution to the
Leibniz-Konferenz 'Nanoscience 2012'
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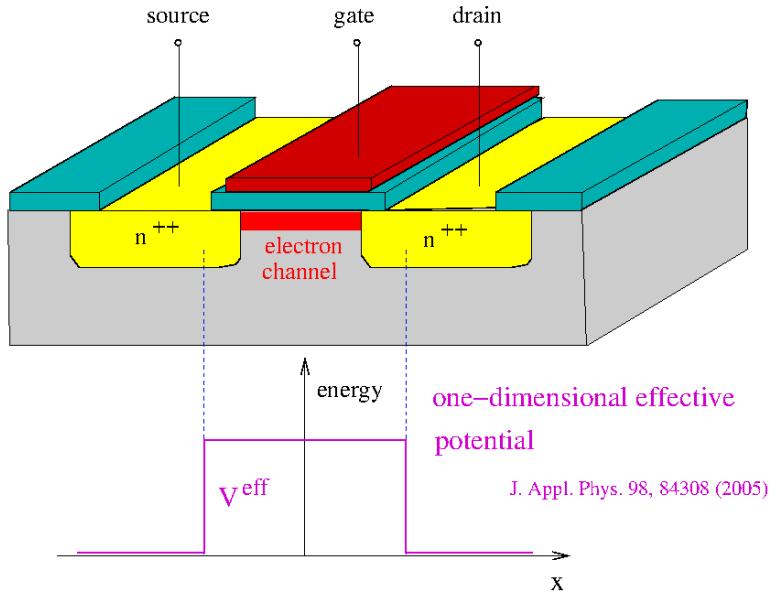
Outline of the presentation

- I. Scale-invariant one-dimensional effective model for quantum transport in nano-transistors
- II. Qualitative comparison with experimental drain characteristics
- III. Calibration of the model parameters: towards quantitative understanding
- IV. Three-parameter calibration for threshold- and subthreshold regime

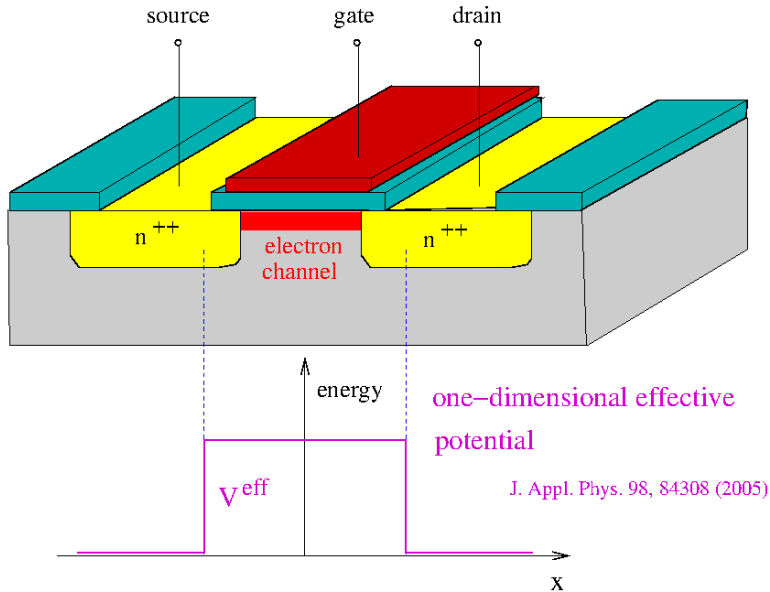
I.1. One-dimensional effective potential



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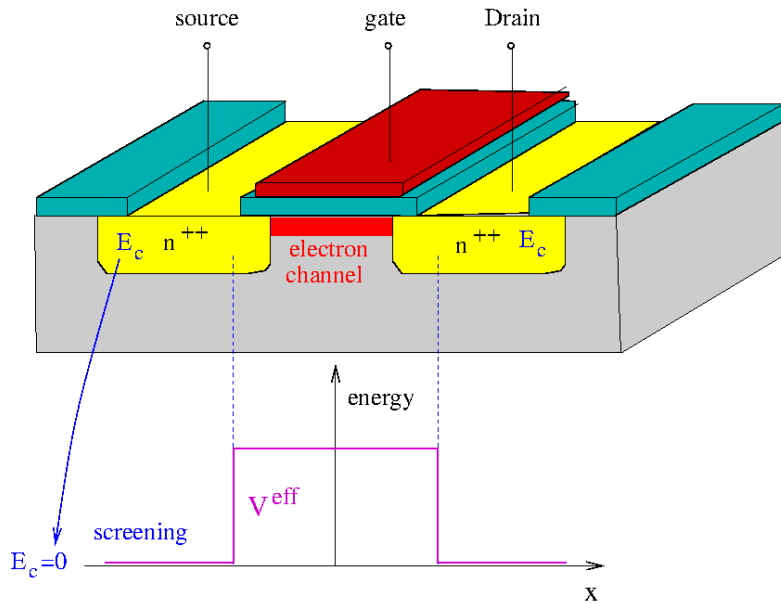


I.1. One-dimensional effective potential

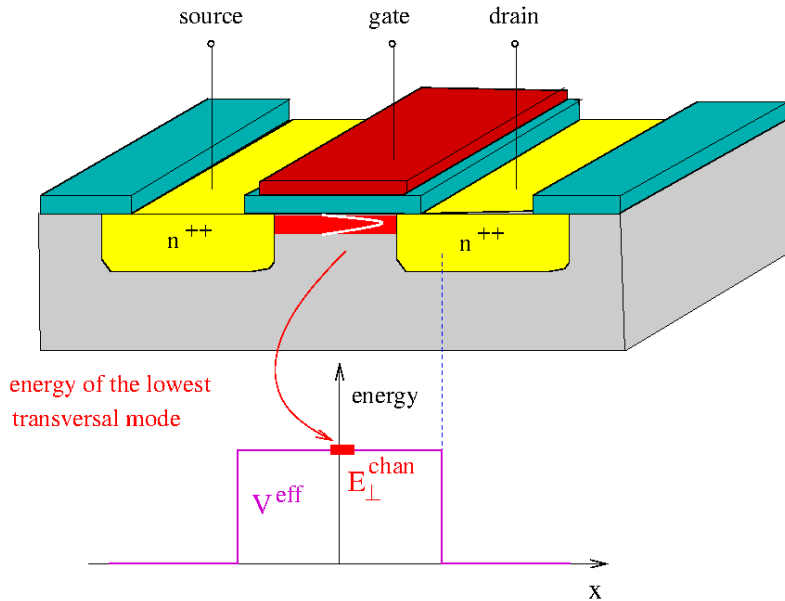


'SMAT'-approximation= single-mode-abrupt-transition

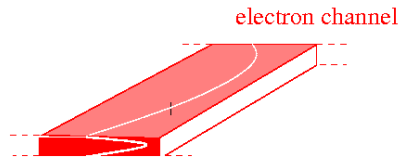
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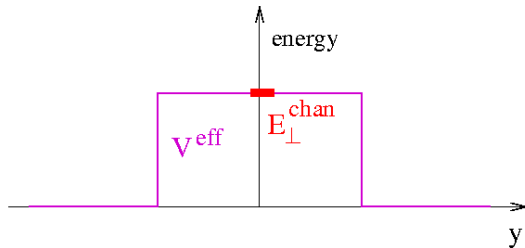
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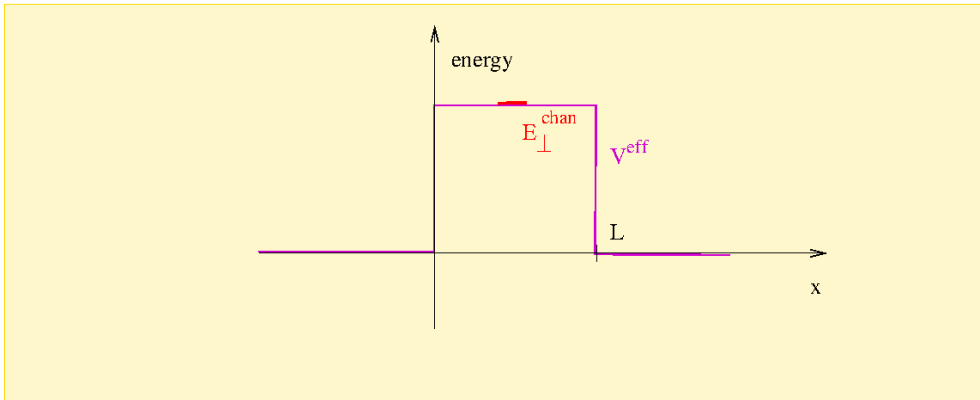


E_{\perp}^{chan} : corresponds to lowest energy with propagating waves
in the 'electron wave-guide'



I.2. One-dimensional effective Schrödinger equation

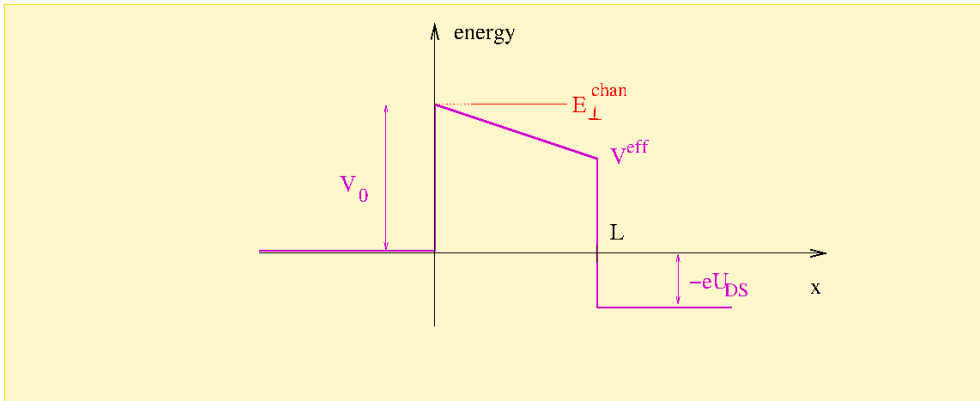
$$\left[-\frac{\hbar^2}{2m^*} \frac{d^2}{dx^2} + V^{eff}(x) - E \right] \psi(x) = 0,$$



I.3. One-dimensional effective problem with drain voltage

$$\left[-\frac{\hbar^2}{2m^*} \frac{d^2}{dx^2} + V^{eff}(x) - E \right] \psi(x) = 0,$$

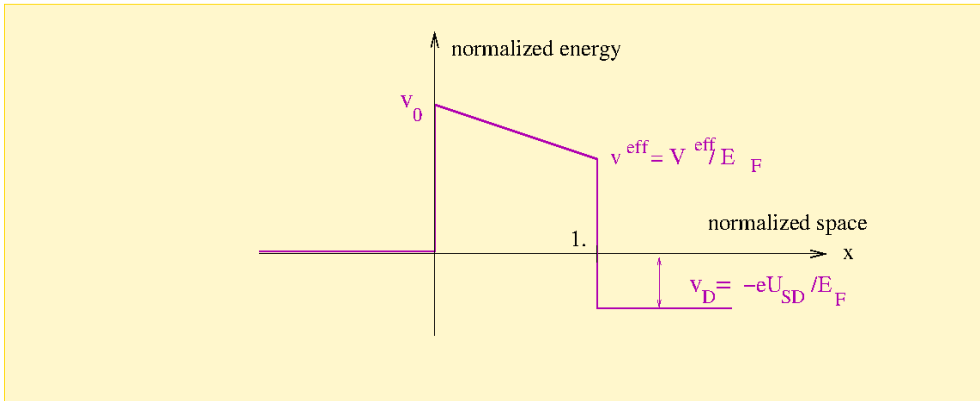
$$V^{eff}(y) = \begin{cases} 0, & \text{for } x < 0 \\ V_0 - \frac{x}{L}eU_{DS} & \text{for } 0 \leq x \leq L \\ -eU_{DS}, & \text{for } x > L. \end{cases}$$



I.4. Scale-invariant representation of the Schrödinger equation

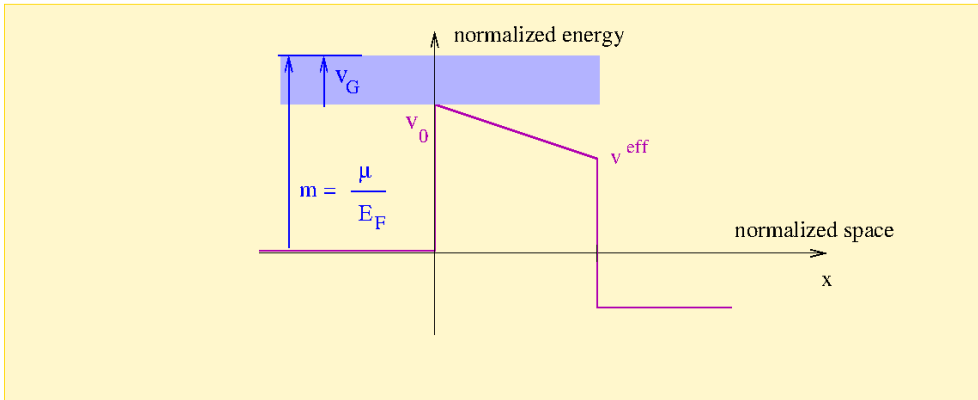
$$\left(-\frac{1}{l^2} \frac{d^2}{dx^2} + v^{eff}(x) - \epsilon \right) \psi(x) = 0$$

$$\frac{x}{L} \rightarrow x \quad \frac{V^{eff}(x)}{E_F} \rightarrow v^{eff}(x) \quad \epsilon = \frac{E}{E_F} \quad l^2 = \frac{2m^* E_F L^2}{\hbar^2}$$



I.5. Introduction of the gate voltage parameter v_G

$$\left(-\frac{1}{l^2} \frac{d^2}{dx^2} + v^{eff}(x) - \epsilon \right) \psi(x) = 0$$



$$v_G = m - v_0$$

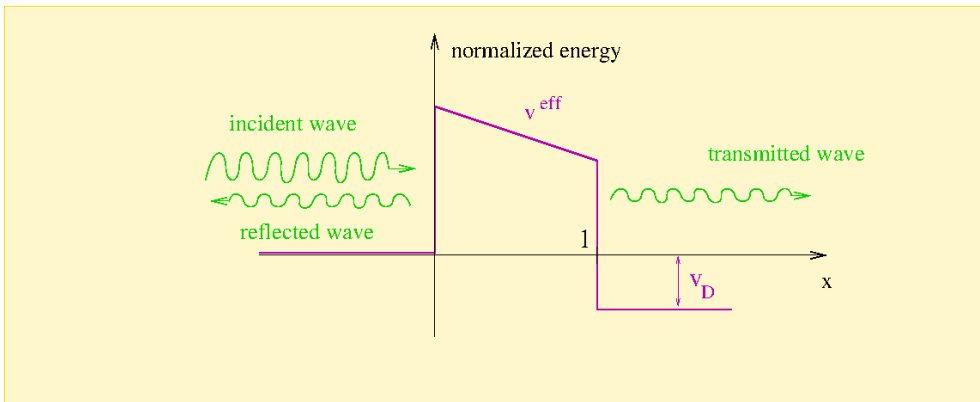
$v_G \gtrsim 0$: ON-state

$v_G \lesssim 0$: quasi-OFF-state

I.6. Scaled current transmission

$$\left(-\frac{1}{l^2} \frac{d^2}{dx^2} + v^{eff}(x) - \epsilon \right) \psi(x) = 0$$

- Source-emitted scattering state $\psi(x \geq 1, \epsilon) = t \exp(ik_D x)$
- Current transmission $T = k_D |t|^2 k_S^{-1}$, $k_D = \sqrt{l^2(\epsilon + v_D)}$



I.7. The scale-invariant Tsu-Esaki formula for drain current

$$j = \frac{I_D}{WJ_0} = \int_0^\infty d\epsilon [s(\epsilon - m) - s(\epsilon - m + v_D)] T(\epsilon)$$

- normalized chemical potential $m = \mu/\epsilon_F$ and $u = k_B T/E_F$

$$m(u) = u X_{\frac{1}{2}} \left(\frac{4}{3\sqrt{\pi}} u^{-3/2} \right), \quad X_{\frac{1}{2}}: \text{inverse F.-D. integral}$$

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- normalized supply function

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- scale-invariant expression for drain current

$$j = j(v_D, v_G, u, l)$$

$$v_D = eU_D/E_F, v_G = V_G/E_F, u = k_B T/E_F, l = L/\lambda \quad (\lambda = \hbar/\sqrt{2m^*E_F})$$

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$$j = \frac{I_D}{W J_0} = \int_0^\infty d\epsilon [s(\epsilon - m) - s(\epsilon - m + v_D)] T(\epsilon) = j(v_D, v_G, u, l),$$

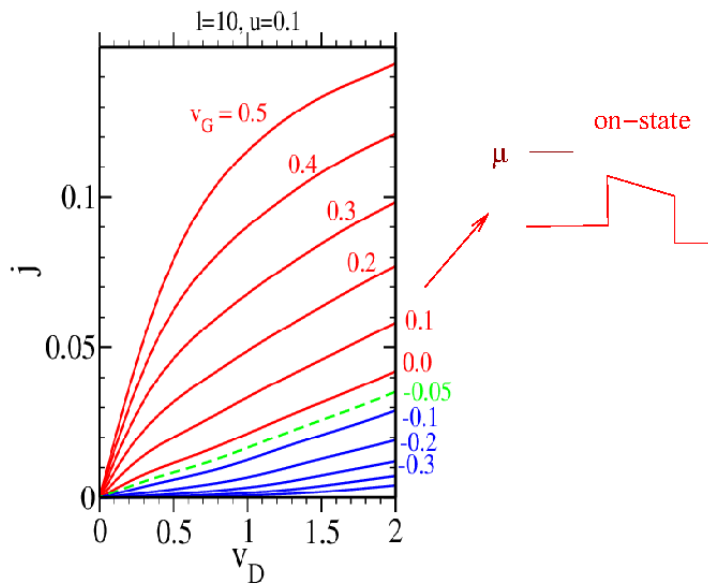
with

$$v_D = eU_D/E_F, \quad v_G = V_G/E_F, \quad u = k_B T/E_F, \quad l = L/\lambda$$

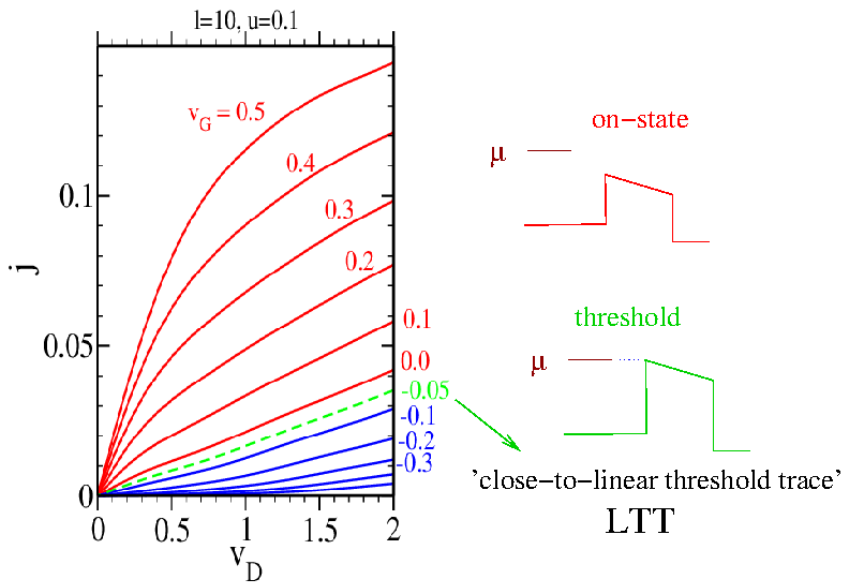
For a wide transistor with strong doping in source/drain contact:

- $E_F = 0.35\text{eV} \Rightarrow u \sim 0.1$ at room temperature
- scaling length $\lambda \sim 1\text{nm}$
- current unit $J_0 = 5.4 \times 10^{-2} \text{A}/\mu\text{m}$

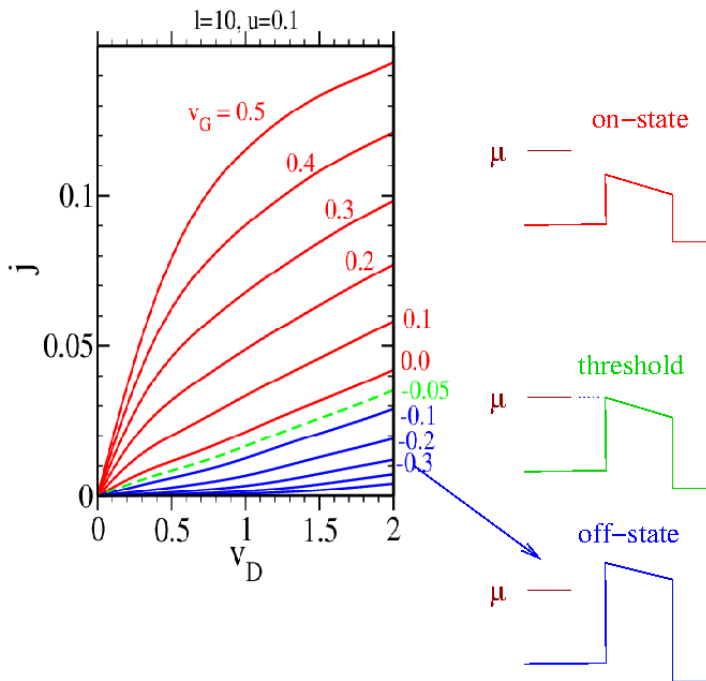
II.1. Theoretical drain characteristics \sim room temperature



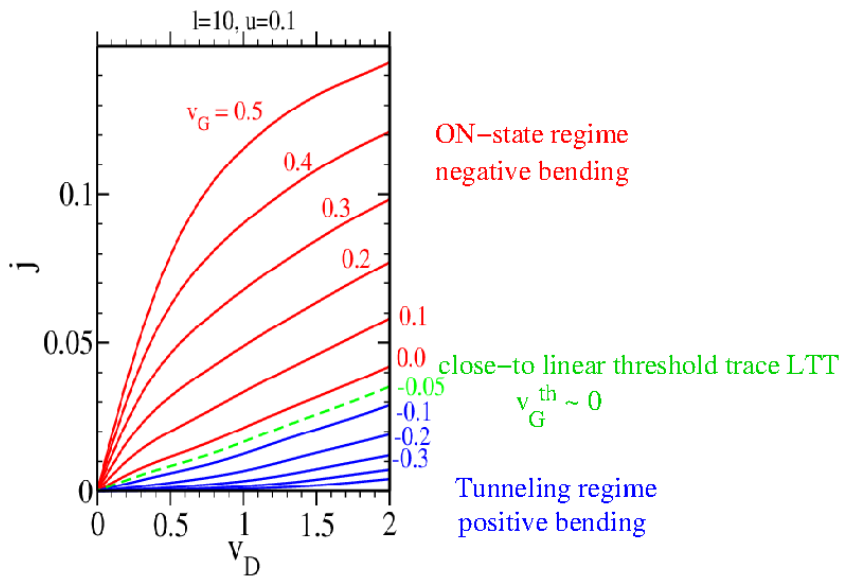
II.1. Theoretical drain characteristics



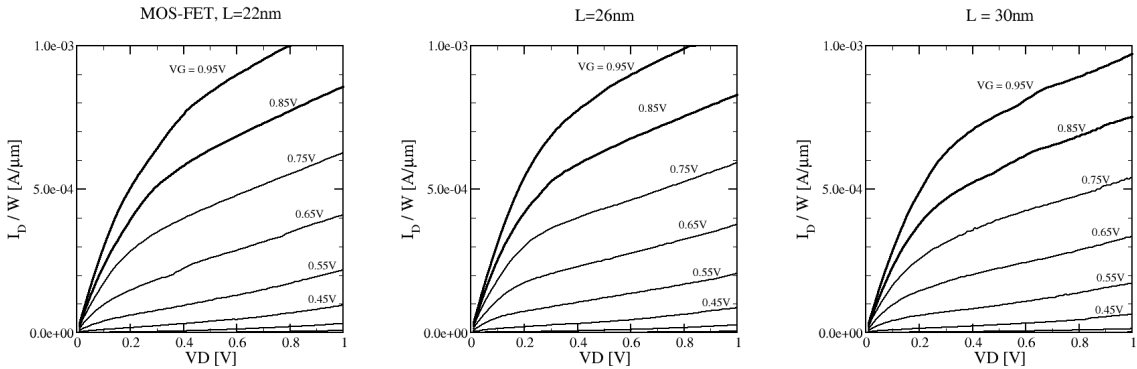
II.1. Theoretical drain characteristics



II.2. Theoretical drain characteristics - qualitative features

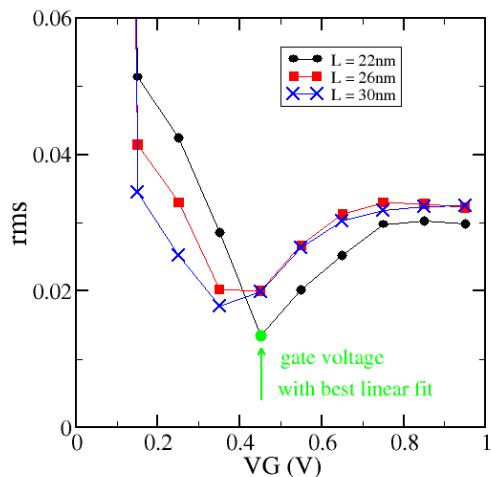
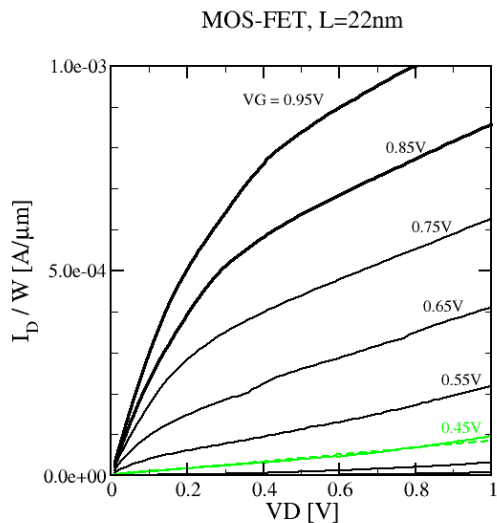


II.3. Experimental drain characteristics



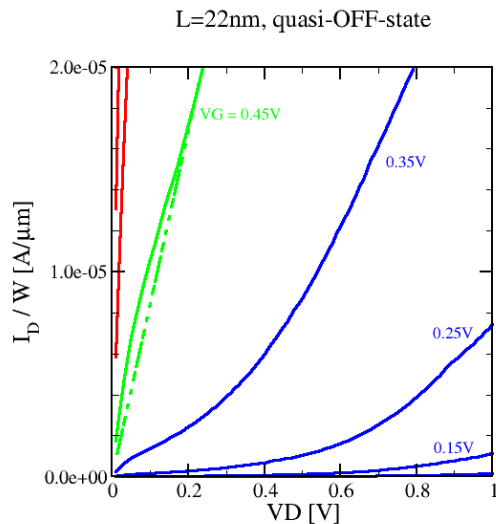
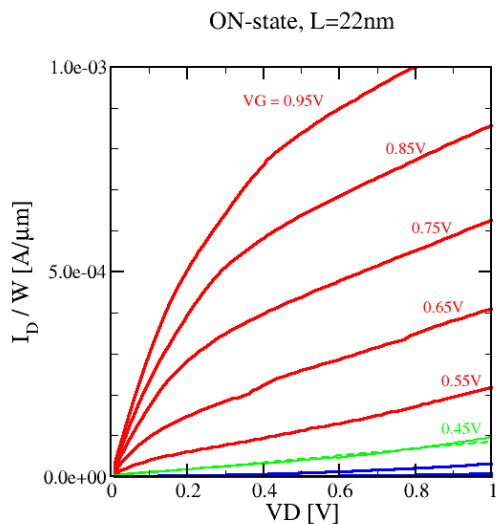
- Transistor data provided by GLOBALFOUNDRIES, Dresden
- $\lambda = 1\text{nm} \Rightarrow L = 22\text{nm}, 26\text{nm}, 30\text{nm}$ corresponds to $l = 22, 26, 30$
- $E_F = 0.35\text{eV} \Rightarrow$ room temperature corresponds to $u \sim 0.1$

II.4. Experimental close-to-linear threshold trace (LTT)



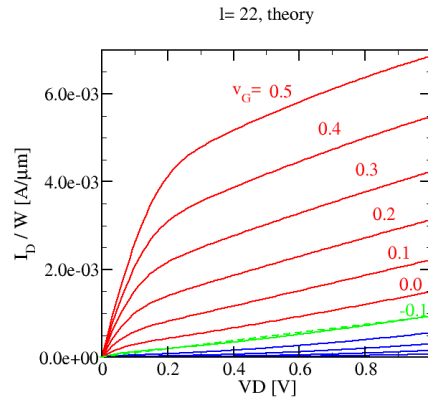
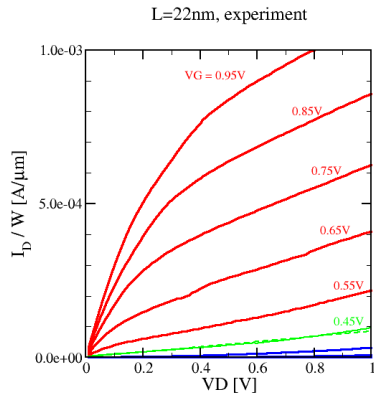
$$\text{rms}(V_G) = \text{Min}_\sigma \left\{ \sqrt{\sum_{V_D} \frac{[I_D(V_D, V_G) - \sigma V_D]^2}{I_D(V_D, V_G)^2}} \right\}$$

II.5. Experimental ON-state and quasi-OFF-state regime



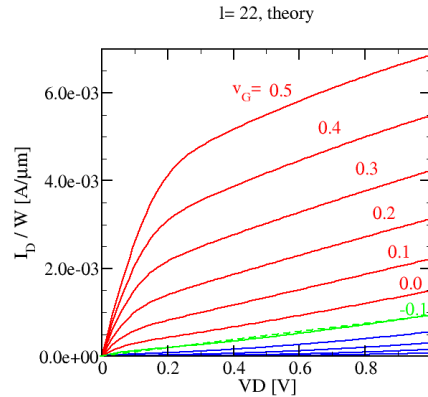
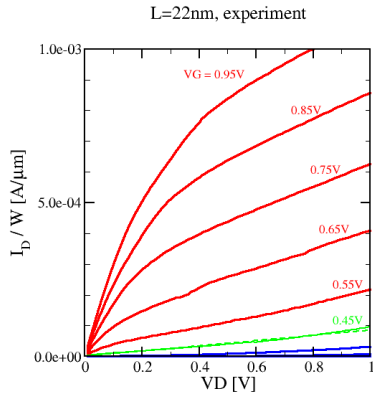
- ON-state negative bending, quasi-OFF-state positive bending

II.6. Comparison theory - experiment without calibration



1. Theoretical LTT-current is bigger than the experimental one
2. For large gate voltages the experimental trace is much smoother
3. No relation between the theoretical v_G and experimental V_G

III.1. Calibration parameters



1. Theoretical LTT-current is bigger than the experimental one
 \Rightarrow current calibration function $I_{cal}(VG)$: $I_D/W = J_0 j \rightarrow I_{cal} J_0 j$
2. For large gate voltages the experimental trace is much smoother
 \Rightarrow heating: temperature calibration function $u(VG)$ is introduced
3. No relation between the theoretical v_G and experimental VG
 \Rightarrow gate calibration function $v_G(VG)$

III.2. Calibration of fit-parameters I_{cal} , u , and v_G

- Fit of the calibrated theoretical current

$$J = \frac{I_D}{W} = I_{cal} J_0 j(v_D, v_G, u, l)$$

to the experimental trace

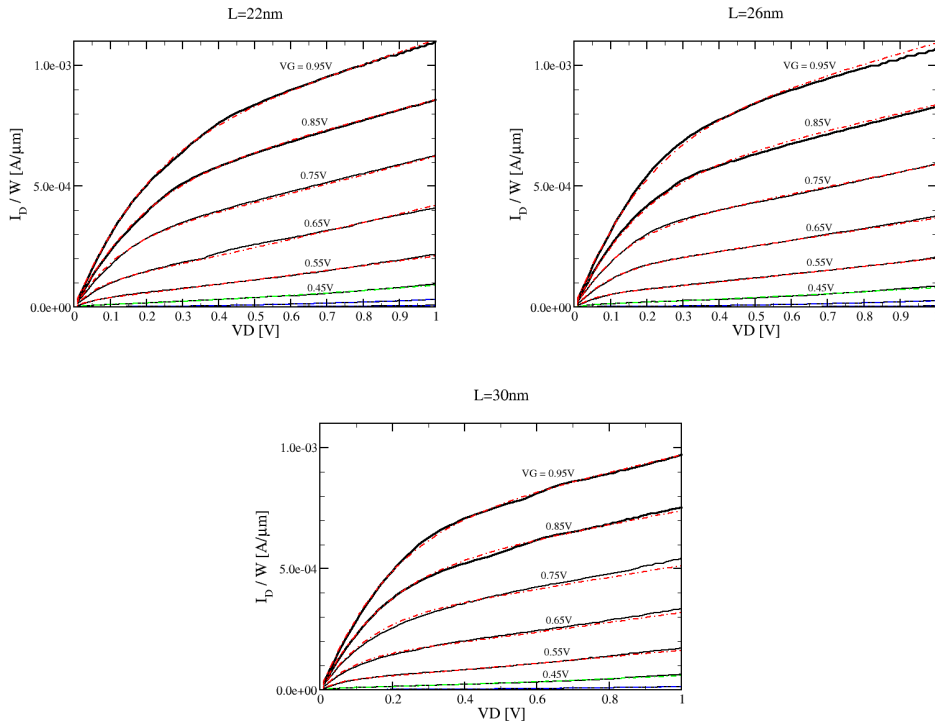
$$J^{exp}(VD, VG, L)$$

at given VG , L , and $l = L/\lambda$, $\lambda = 1nm$

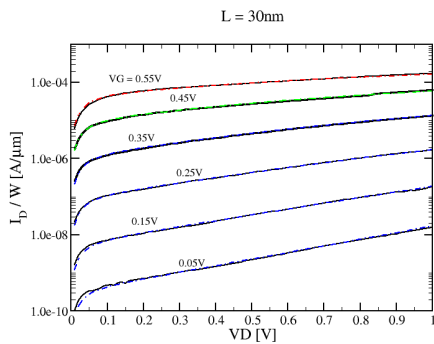
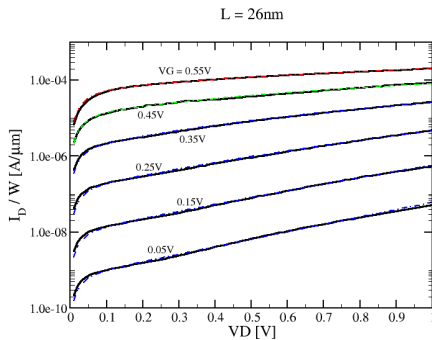
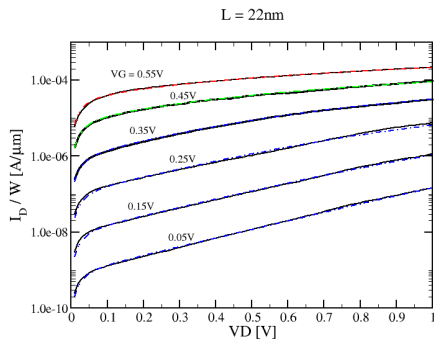
- Minimization of the root mean square sum

$$\text{rms}(I_{cal}, u, v_G) = \sum_{VD} \frac{[J^{exp}(VD, VG, L) - I_{cal} J_0 j(VD/E_F, v_G, u, L/\lambda)]^2}{J^{exp}(VD, VG, L)^2}$$

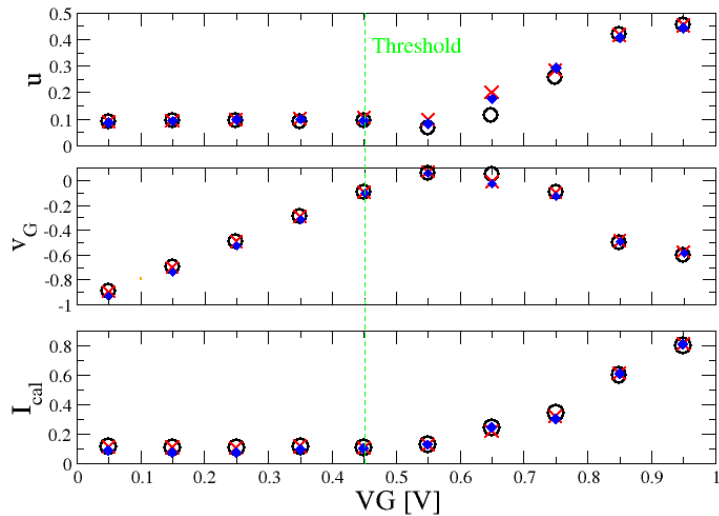
III.3. Theory vs. experiment with calibration in ON-state



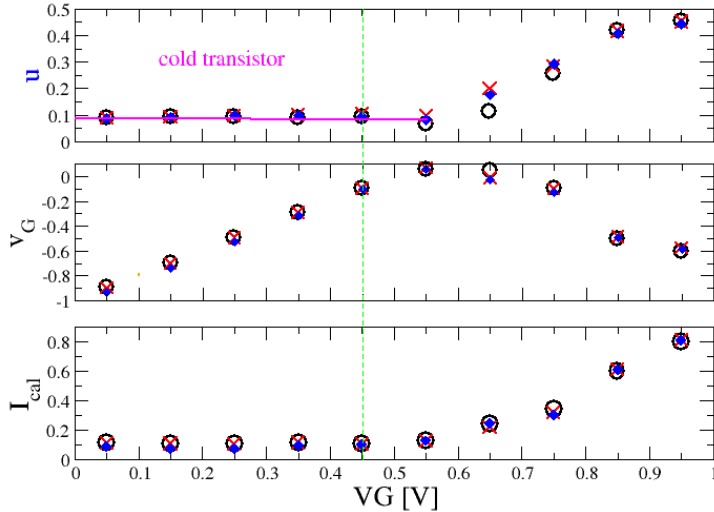
III.4. Theory vs. experiment in quasi-OFF-state



III.5. Results for the calibration functions

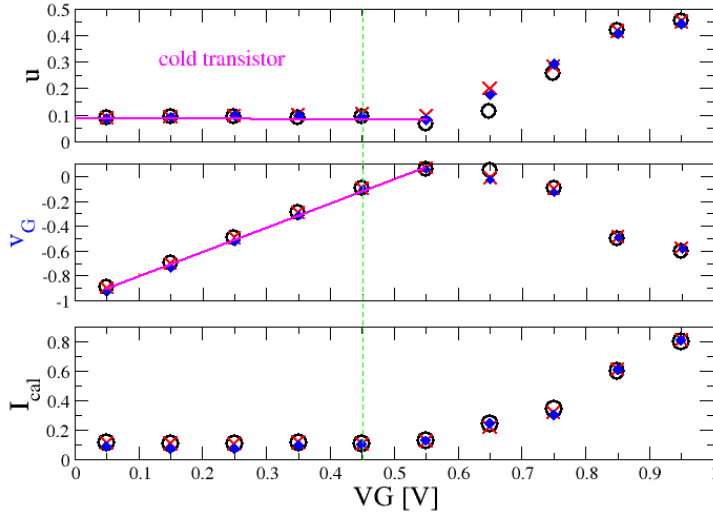


III.5. Results for the calibration function



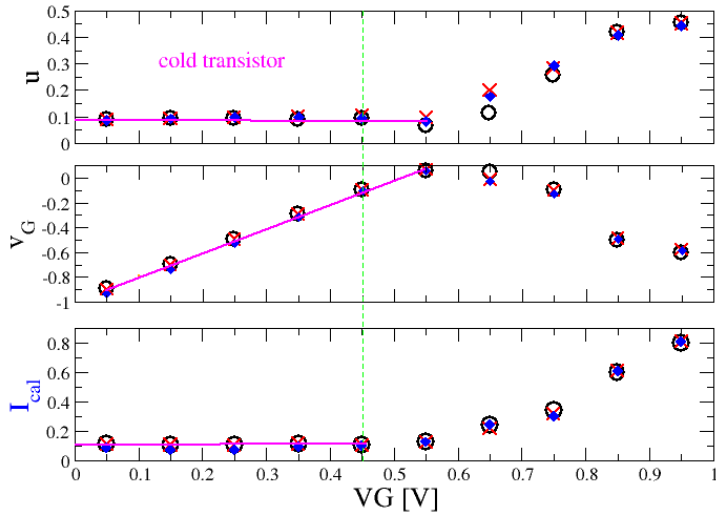
- subthreshold- and threshold regime: small drain current \Rightarrow room temperature ('cold transistor'). ON-state: increased drain current \Rightarrow dissipation and heating. Traces more rounded than at room temperature

III.5. Results for the calibration function



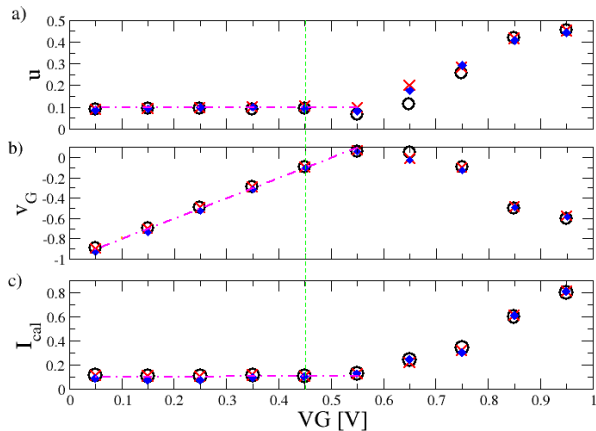
- cold transistor: $\mu \sim E_F \Rightarrow v_G = m - v_0 \sim E_F - v_0 \Rightarrow$ changes in v_0 translate directly into v_G . Constant capacitance $\Rightarrow v_G(V_G)$ is linear.
- hot transistor: chemical potential and v_G drops.

III.5. Results for the calibration function



- Relatively big current calibration constant I_{cal} is to be expected given the simplicity of the model. It depends on the coupling of the contacts to the electron channel.

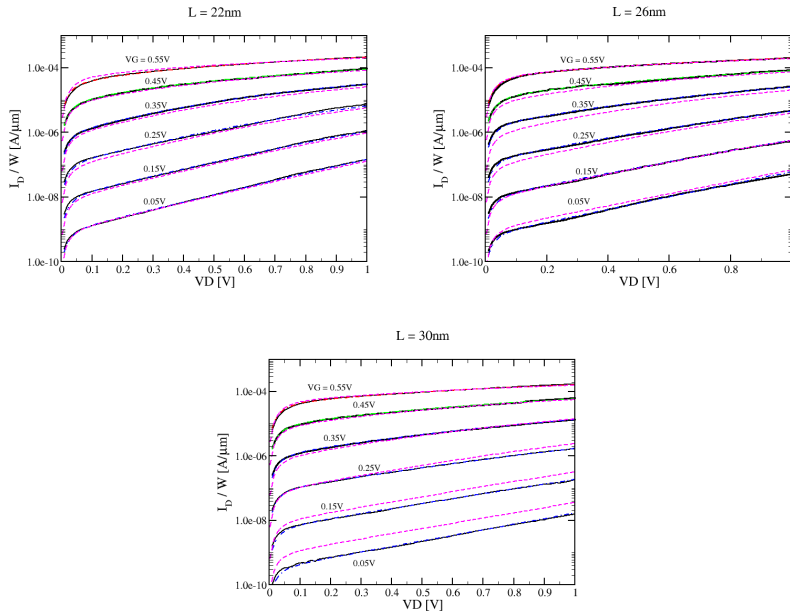
IV.1 Simple three-parameter calibration in quasi-OFF-state



$$v_G(VG < 0.55V) = \alpha(VG - VG_T) + v_T$$

In magenta: $u = 0.09$ (room temperature), $\alpha = 2.0$ (constant capacitance of the electron channel), and $I_{cal} = 0.1$.

IV.2 Three-parameter calibration comparison with experiments



In magenta: $u = 0.09$, $\alpha = 2.0$, and $I_{cal} = 0.1$.

V. Conclusion

- Presentation of a scale-invariant one-dimensional effective model for quantum transport in nano-transistors
- Qualitative comparison with experimental drain characteristics: ON-state regime (traces with negative bending), close-to linear threshold characteristic (LTT), quasi-OFF-state tunneling regime (traces with positive bending)
- Calibration of the model parameters yields quantitative description
 - temperature calibration \Rightarrow heating of transistor in ON-state
 - gate voltage calibration \Rightarrow capacitance model of nanotransistor
 - current calibration \Rightarrow optimization of transition of wave functions between contacts and transistor channel
- Simple three-parameter calibration for threshold- and subthreshold regime is possible